

# Reasoning and Problem Solving

## Step 5: What is Volume?

### National Curriculum Objectives:

Mathematics Year 5: (5M8) [Estimate volume \[for example, using 1 cm<sup>3</sup> blocks to build cuboids \(including cubes\)\] and capacity \[for example, using water\]](#)

Mathematics Year 5: (5M9a) [Use all four operations to solve problems involving measure \[for example, length, mass, volume, money\] using decimal notation, including scaling](#)

### Differentiation:

Questions 1, 4 and 7 (Problem Solving)

**Developing** Find two possible shapes where the length, width and depth equal a volume less than 8cm<sup>3</sup>

**Expected** Find three possible shapes where the length, width and depth equal a volume of 10cm<sup>3</sup>

**Greater Depth** Find five possible shapes where the length, width and depth equal a volume less than 20cm<sup>3</sup>

Questions 2, 5 and 8 (Problem Solving)

**Developing** Find the odd one out by matching two shapes to three possible volumes.

**Expected** Find the odd one out by matching three shapes to four possible volumes.

**Greater Depth** Find the odd one out by matching four shapes to five possible volumes.

Questions 3, 6 and 9 (Reasoning)

**Developing** Explain which shape has the greatest volume when choosing from two simple statements.

**Expected** Explain which shape has the greatest volume when choosing from two statements.

**Greater Depth** Explain which shape has the greatest volume when choosing from three statements.

More [Year 4 and Year 5 Area and Volume](#) resources.

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# Reasoning and Problem Solving – What is Volume?

1a. Sophie makes a shape that has a volume of  $8\text{cm}^3$ .



What does my shape look like?

Find two different shapes with the same volume as Sophie.



5 PS

1b. Damon makes a shape that has a volume of less than  $8\text{cm}^3$ .



What does my shape look like?

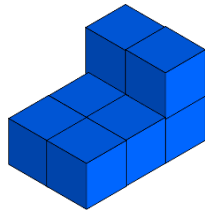
Find two different shapes with a volume less than  $8\text{cm}^3$ .



5 PS

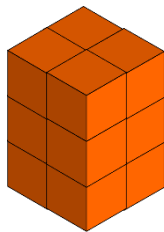
2a. Find the odd one out by matching the shape and the volume.

$12\text{cm}^3$



$8\text{cm}^3$

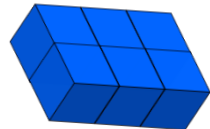
$14\text{cm}^3$



5 PS

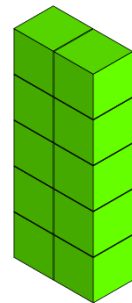
2b. Find the odd one out by matching the shape and the volume.

$12\text{cm}^3$



$10\text{cm}^3$

$6\text{cm}^3$



5 PS

3a. Which child has the greatest volume?

Joel



My shape has a length of 2 cubes, a width of 2 cubes and a height of 2 cubes.

My shape has a length of 3 cubes, a width of 1 cube and a height of 2.



Adam

Explain.



5 R

3b. Which child has the greatest volume?

Milly



My shape has a length of 3 cubes, a width of 1 cube and a height of 3 cubes.

My shape has a length of 2 cubes, a width of 3 cube and a height of 2.



Tom

Explain.



5 R

# Reasoning and Problem Solving – What is Volume?

4a. Isla makes a shape that has a volume of  $10\text{cm}^3$ .



What does my shape look like?

Find three different shapes with a volume of  $10\text{cm}^3$ .



5 PS

4b. Jake makes a shape that has a volume of less than  $10\text{cm}^3$ .



What does my shape look like?

Find three different shapes with a volume of less than  $10\text{cm}^3$ .



5 PS

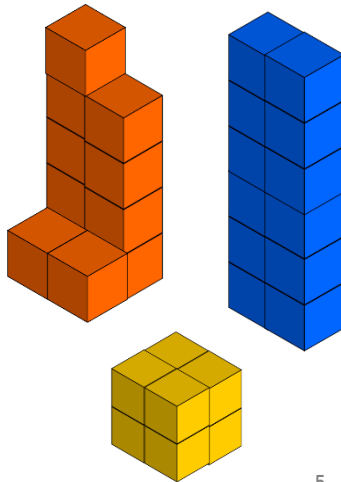
5a. Find the odd one out by matching the shape and the volume.

$8\text{cm}^3$

$16\text{cm}^3$

$12\text{cm}^3$

$11\text{cm}^3$



5 PS

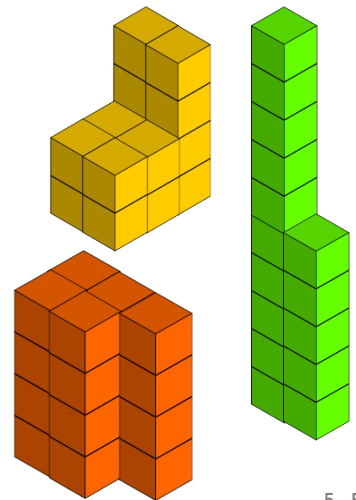
5b. Find the odd one out by matching the shape and the volume.

$15\text{cm}^3$

$16\text{cm}^3$

$17\text{cm}^3$

$20\text{cm}^3$



5 PS

6a. Which child has the greatest volume?

Tyler



My shape has a length of 4 cubes, a width of 2 cubes and a height of 2 cubes.

My shape has a length of 6 cubes, a width of 2 cubes and a height of 2 cubes.



Meera

Explain.



5 R

6b. Which child has the greatest volume?

Phoebe



My shape has a length of 5 cubes, a width of 2 cubes and a height of 3 cubes.

My shape has a length of 7 cubes, a width of 2 cubes and a height of 2 cubes.



Jason

Explain.



5 R

# Reasoning and Problem Solving – What is Volume?

7a. Abdalla makes a shape that has a volume of between  $10\text{cm}^3$  and  $20\text{cm}^3$ .



What does my shape look like?

Find five different shapes with a volume of less than  $20\text{cm}^3$ .



5 PS

7b. Alison makes a shape that has a volume of less than  $20\text{cm}^3$ .



What does my shape look like?

Find five different shapes with a volume of less than  $20\text{cm}^3$ .



5 PS

8a. Find the odd one out by matching the shape and the volume.

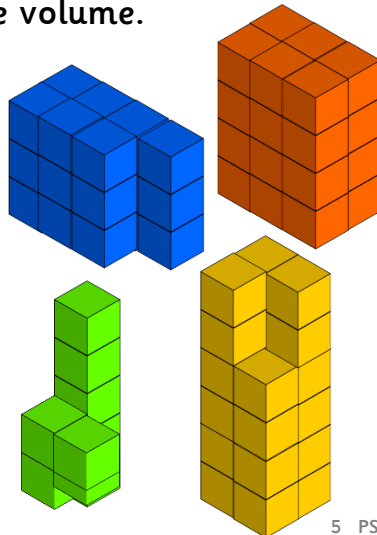
$21\text{cm}^3$

$18\text{cm}^3$

$24\text{cm}^3$

$16\text{cm}^3$

$22\text{cm}^3$



5 PS

8b. Find the odd one out by matching the shape and the volume.

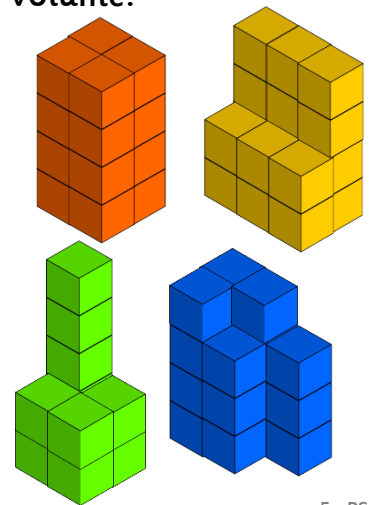
$11\text{cm}^3$

$21\text{cm}^3$

$16\text{cm}^3$

$18\text{cm}^3$

$20\text{cm}^3$



5 PS

9a. Which child has the greatest volume?

Amy



My shape has a length of 3 cubes, a width of 5 cubes and a height of 3 cubes.

My shape has a length of 4 cubes, a width of 6 cubes and a height of 2 cubes.

Sam



Sara



My shape has a length of 4 cubes, a width of 4 cubes and a height of 3 cubes.

Explain.



5 R

9b. Which child has the greatest volume?

Maria



My shape has a length of 8 cubes, a width of 1 cubes and a height of 4 cubes.

My shape has a length of 3 cubes, a width of 6 cubes and a height of 2 cubes.

Zac



Chen



My shape has a length of 4 cubes, a width of 3 cubes and a height of 2 cubes.

Explain.



5 R

# Reasoning and Problem Solving – What is Volume?

## Developing

- 1a. Any shape built from eight  $1\text{cm}^3$  cubes.
- 1b. Any shape built from one to seven  $1\text{cm}^3$  cubes.
- 2a.  $14\text{cm}^3$  is the odd one out.
- 2b.  $12\text{cm}^3$  is the odd one out.
- 3a. Joel is correct as his shape has a volume of  $8\text{cm}^3$ . The volume of Adam's shape is  $8\text{cm}^3$ .
- 3b. Tom is correct as his shape has a volume of  $12\text{cm}^3$ . The volume of Milly's shape is  $9\text{cm}^3$ .

## Expected

- 4a. Any shape built from ten  $1\text{cm}^3$  cubes.
- 4b. Any shape built from one to nine  $1\text{cm}^3$  cubes.
- 5a.  $16\text{cm}^3$  is the odd one out.
- 5b.  $17\text{cm}^3$  is the odd one out.
- 6a. Meera is correct as her shape has a volume of  $24\text{cm}^3$ . The volume of Tyler's shape is  $16\text{cm}^3$ .
- 6b. Phoebe is correct as her shape has a volume of  $30\text{cm}^3$ . The volume of Jason's shape is  $28\text{cm}^3$ .

## Greater Depth

- 7a. Any shape built using between ten and twenty  $1\text{cm}^3$  cubes.
- 7b. Any shape built using between one and nineteen  $1\text{cm}^3$  cubes.
- 8a.  $18\text{cm}^3$  is the odd one out.
- 8b.  $20\text{cm}^3$  is the odd one out.
- 9a. Sam and Sara are correct as their shapes have a volume of  $48\text{cm}^3$ . The volume of Amy's shape is  $45\text{cm}^3$ .
- 9b. Zac is correct as his shape has a volume of  $36\text{cm}^3$ . The volume of Maria's shape is  $32\text{cm}^3$ . The volume of Chen's shape is  $24\text{cm}^3$ .